SECURE OUTSOURCING

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DEFINITIONS

C has data and a task (a problem).
A has hardware and appropriate software (a server).

Outsourcing: C sends problem to A.
A computes a solution and returns answer to C.

Secure Outsourcing: A never knows the problem or its solution.

Mutually Secure Outsourcing: $C_1$ and $C_2$ send parts of the problem to $A$ who returns the solution to both. $C_1$ and $C_2$ do not learn each others problem data, $A$ still knows nothing.
**Problem**: Compute \( \int_{1}^{a} f(x) \, dx \).

- Disguise problem by choosing a random function \( s(x) \) of smooth piecewise cubics.
- Send \( A \) the problem: Compute \( \int_{1}^{9} [f(x) + s(x)] \, dx \) and get \( I \) back.

3. Find answer \( I - \int_{1}^{9} s(x) \, dx \). It is trivial to integrate \( s(x) \).
SECURE OUTSOURCING REQUIRES

- A cheap way to disguise the problem.
- A cheap way to unveil the answer.
- A disguise that is completely secure.
A REAL EXAMPLE: Matrix Multiplication $M_1M_2$

**Step 1:** Create 3 random permutations of $1 \rightarrow N$ and 3 sets of random, non-zero numbers.

**Step 2:** Put the numbers into the non-zero places of the permutation matrices $P_1$, $P_2$, and $P_3$.

**Step 3:** Compute $X = P_1M_1P_2^{-1}$, $Y = P_2M_2P_3^{-1}$.

**Step 4:** Outsource problem $Z = XY$.

**Step 5:** Compute $P_1^{-1}ZP_3$ which is $M_1M_2$.

Work of Steps 1, 2, 3 and 5 is order $N^2$. Work of Step 4 is order $N^3$. $X$, $Y$ and $Z$ reveal nothing about $M_1$ and $M_2$. 
Disguise makes a functional or mathematical transformation of the entire object. It preserves distance and is really a “floating point” methodology. Encryption processes the symbols of an object and destroys distance.

Secure Outsourcing is a form of Secure Multi-party Computing which uses disguise instead of the usual encryption.
How general is outsourcing disguise? One can do:

- **Linear algebra**: Multiplication, Inversion, Solve $Ax = b$, Convolution, etc.
- **Sorting**.
- **Calculus**: integration, differential equations, transforms.
- **Matching**: Strings, approximate templates, images.

The work to do the disguise and unveil the answer is small compared to the problem solving. The server’s work is comparable to the work without disguise.
KEY QUESTION TWO

How secure is the outsourcing disguise? Our studies suggest the disguises can be made unbreakable to:

- Statistical attacks (try to find the random numbers, functions, mappings,..)
- Approximation theory attacks (try to discover the function behaviors).
- Symbolic code attacks (try to decipher the problem text).
KEY QUESTION THREE

How broad are the applications of disguise? Is it only applicable to scientific computations?

**Answer 1**: There are some substantial direct applications.

- Schlumberger seismic data analysis service.
- Pattern matching.
  - Was your son caught on the video tapes of the Purdue riots?
  - Is there an oil well being drilled in Benton county?
  - Is a variation of my program being used in MS word?
- Device design.
  - Will your new windmill really be 150% more efficient?

**Answer 2**: Mutually secure disguises have much broader applications.
MUTUALLY SECURE OUTSOURCING APPLICATIONS

- Joint seismic exploration.
- Joint device design.
  - These are impractical without such a technology.
- Medical diagnosis (records compared to symptoms).
  - Does anyone here have AIDS? Leprosy?
  - What’s wrong with my daughter?
- Biometric identification (characteristics compared to records).
  - Do your fingerprints match those on the gun?
  - Are your Mike Atallah?
How would this work in practice?

**Sophisticated Users:** A problem solving environment would allow the “programming” of disguises using high level, built-in operators (random functions, key management, symbolic transformations, domain transformations, one time random sequences,…)

**Ordinary Applications:** A fixed disguise program handles everything for a particular application. The only input is a key and the information. The program may be embedded in a device.