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PR-DRA: PageRank-based defense resource allocation methods for securing interdependent systems modeled by attack graphs

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Introduction

• We focus on developing proactive defense framework to counteract the huge amount of different cyberattacks targeting interconnected systems.

• We utilize an evolutionary optimizer, called Genetic Algorithm (GA), for identifying different potential attack routes that attackers are likely to leverage in their attacks.

PR-DRA - Evaluation

Datasets	System	# Nodes	# Edges	# Critical Assets	Graph Type
Dalasels	SCADA	13	20	6	directed
	DER.1	22	32	6	directed
	E-Commerce	20	32	4	directed
	VOIP	22	35	4	directed

- We use the popular Google's PageRank (PR) algorithm to determine the significance of each asset node (critical asset) and define the security proportion that should be allocated to protect it.
- We propose four graph-theoretic approaches to mitigate attacks like stepping-stone, cascading failure, single node, and multi-stage attack on interdependent systems.
- We demonstrate an end-to-end framework that combines PageRank with four mitigation methods for enhancing attack resilience and interdependent systems protection.

Motivation

- The lack of efficient resource allocation approaches has led to wasted limited resources and resulted in low or poor protection.
- Many studies operate by guessing or assuming the moves that attackers may consider and act upon, which is **difficult** to **predict** in real-world scenarios.
- Developing efficient resource allocation framework designed to minimize cost, maximize protection, and **reduce resource waste** would be **financially** beneficial for organizations.
- Developing high-performance resource allocation approach that operates independently from guessing attackers' strategies and provides high level of security is essential for protecting interdependent systems.

Our Contribution

- The research introduces an end-to-end framework for allocating resources to secure interconnected systems, independent of initial guesses about attackers or their numbers.
- The research uses **PR** algorithm, along with four allocation methods to improve system security levels, in which the **resources allocated** for specific asset is **proportional** to **its normalized rank**.



Convergence of the PageRank with Different Initial Guess for Different Attack Graphs



Comparison with Random (left) and 1s (right) Initial Investments Under Budget of 10 Units

Composite Cost Relative Reduction





• Two different metrics are used to evaluate our methods: PR + In-Degree Nodes, PR + Adjacent Nodes, **PR + Markov Blanket**, and **PR + Min-Cut Edges**, across four real-world systems and five baselines.

• The source code of the **framework** is released to the community as **baseline approach** for **allocating** resources to secure interdependent systems and encourage further development with new methods.

Framework

Modeling Attack and Defense:

• The system is modeled using an attack graph G = (V, E, W), where (V) represents entries, intermediates and assets, (E) represents attack links, and (W) represents weight (initial investments $x_{i,i}$).

 $p_{i,j}$

• Direct edge $(v_i, v_j) \in E$ is occurred when v_i is revealed and then attacking v_i .

• Probability $p_{i,i}(x_{i,i})$ indicates chance of an attacker breaching node v_i from v_i .

• The attack success probability on path P is given by $\prod_{(v_i,v_j)\in P} \exp(-x_{i,j})$.

• The defender *D* is responsible for protecting a set of assets $V_m \subseteq V$.

• If asset v_m is compromised, the defender incurs a financial loss L_m .

• Resources are distributed on a set of edges $(v_i, v_i) \in E$

• The defender D_k minimizes the **cost function**:

$$C_k(x_k, x_{-k}) \triangleq \sum_{v_m \in V_k} L_m\left(\max_{P \in \mathbb{P}_m} \prod_{(v_i, v_j) \in P} p_{ij}(x_{i,j})\right)$$

PageRank-based Security Resource Allocation Framework:

Scalability for the Parallelized GA for Processing Top1 Attack Paths for Different Graphs



PRV1 vs PR(JGraphT) with In-Degree Under Random Initial Investments

Budget = 25 units					
Dataset / System	PRV1	PR (JGraphT)			
SCADA	83.99	79.95			
DER.1	98.07	97.05			
E-Commerce	71.8	97.74			
VOIP	94.69	90			

Budget ≡ 10 units						
Dataset / System	Optimized PR	PR (JGraphT)				
SCADA	63.76	53.49				
DER.1	85.14	80.86				
E-Commerce	94.94	74.96				
VOIP	69.29	66.52				

Key Takeaways

• Creation of a novel end-to-end resource allocation framework for mitigating various attack types in order to secure interdependent systems, regardless of the entry points of attackers, and ensuring the protection of all assets according to their importance.



• PR-DRA Framework still need improvements to be applied in a production environment, but this work is an important step in this direction.

• PageRank's reliance on node connectivity is challenged in complex networks, where critical nodes may have **fewer connections** but **greater importance** (tackled by the optimized version).

• The resource allocation methods can be improved by adopting hybrid independent defenders, where multiple defenders use different allocation techniques in parallel.

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