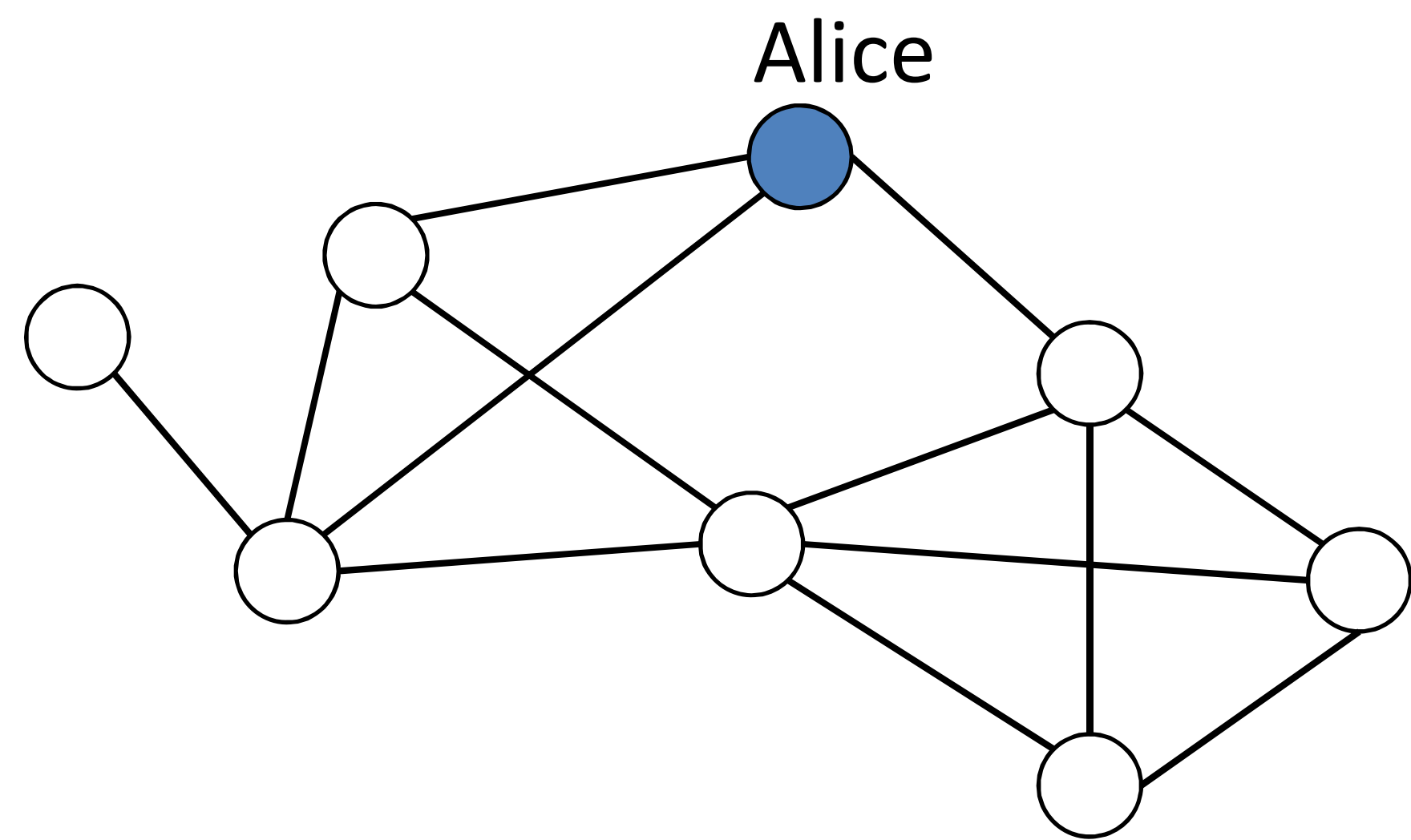


ϵ -Differential Node Privacy in Graph Data Queries

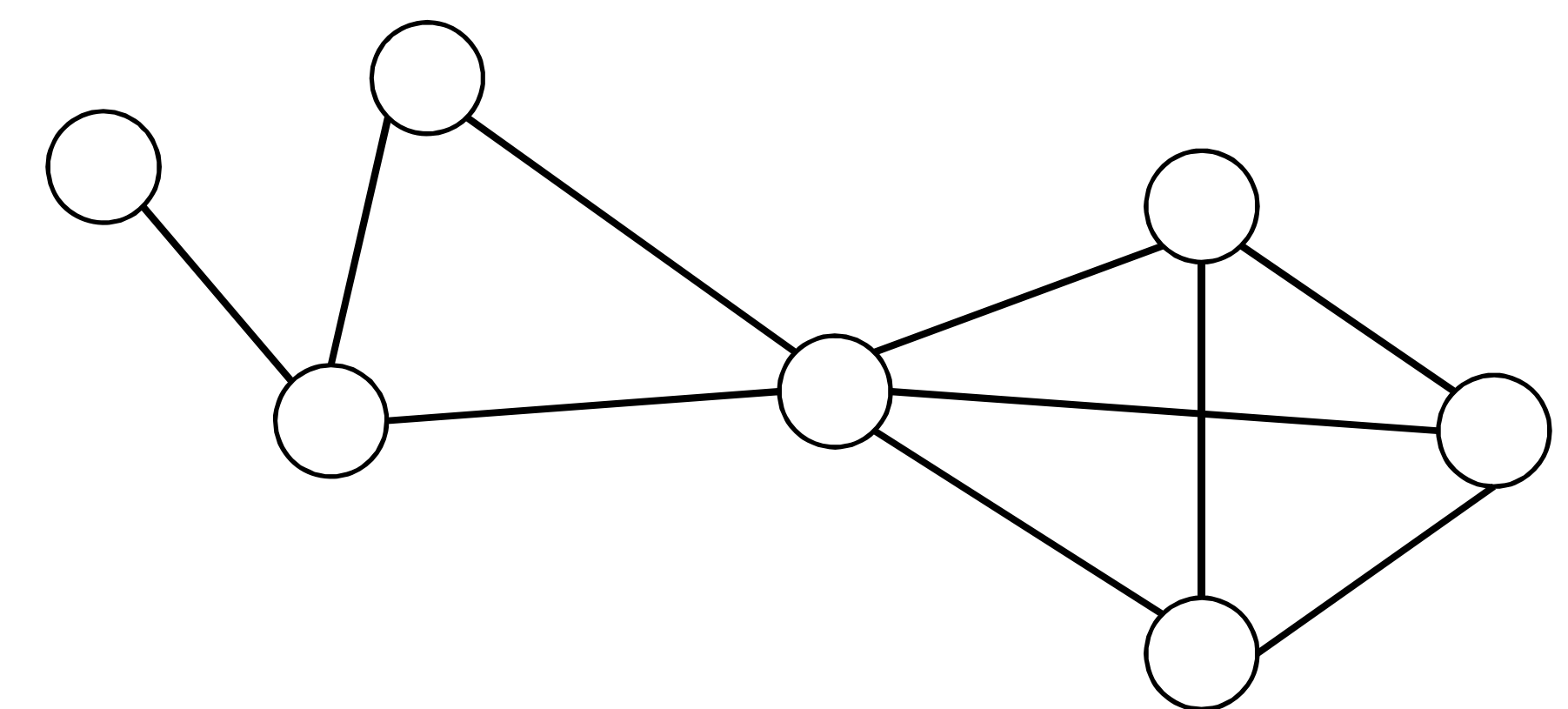
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Min-Cut(G_1) = 2

Friend Network Data:
Nodes = Individuals
Edges = Friendships
Query: What is the smallest number of individuals connecting parts of the graph?

Neighboring Graphs:
Differ in one individual



Min-Cut(G_2) = 1

Differentially Private Min-cut :
Randomized Query Result could be 1.37, 1.80, 1.46, ...

Differential Privacy guarantees sufficient noise that guessing which of the neighboring graphs produced the query result is unlikely. This protects individual privacy: if query results from G_1 and G_2 are indistinguishable, we cannot learn Alice's data.

Query Sensitivity is a measure of the maximum difference between query results on *any* neighboring graphs. High sensitivity queries require adding so much noise that results are useless – hence, we cannot perform such analyses *and* guarantee privacy.

High Sensitivity Queries:

- Graph Isomorphism
- Average Node Degree
- Graph Diameter
- PageRank
- Connected Components

Open Problems:

- Social Cluster Identification
- Propagation Algorithms (popularity measures)
- Subgraph Counting with unique edges

Low Sensitivity Queries:

- Subgraph Counting with unique nodes
- Degree Distribution^[1]
- Min-Cut
- Graph Estimation^[2]

[1] Michael Hay, et al., "Accurate Estimation of the Degree Distribution of Private Networks", IEEE International Conference on Data Mining, 2009

[2] Darakhshan J. Mir and Rebecca N. Wright, "A differentially private graph estimator", International Workshop on Privacy Aspects of Data Mining, 2009.